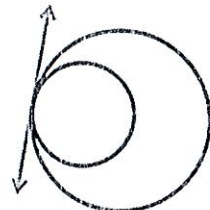


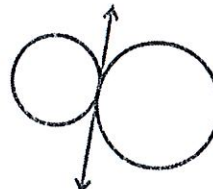
Day 3 – Tangent Properties

Last unit, you learned that tangent lines intersect a circle in exactly one place. This leads to several theorems about tangent lines.

Tangent Circles are two coplanar circles that intersect at exactly one point. They may intersect internally or externally.

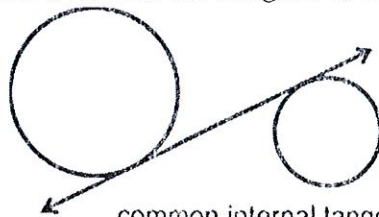


internally tangent



externally tangent

Common Tangent Lines are lines that are tangent to two circles.

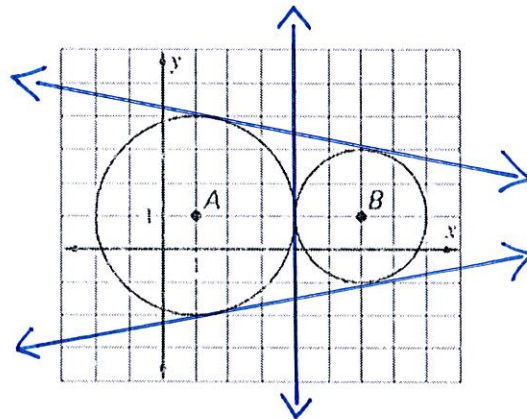


common internal tangent



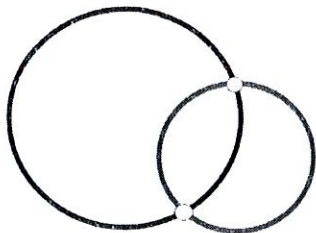
common external tangent

Example: Draw any common tangent lines.

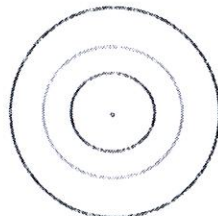


Other Points of Intersection:

Circles may also intersect at two or no points.

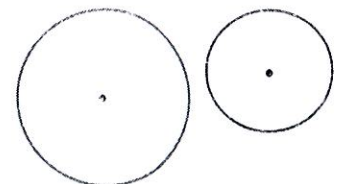


Two Points of Intersection



No Points of Intersection:

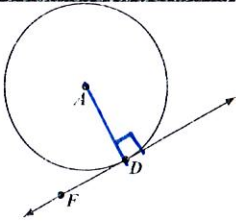
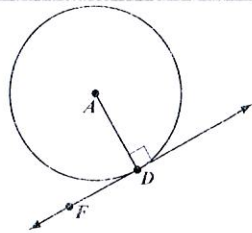
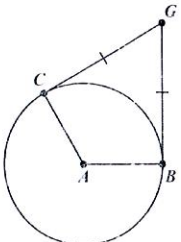
These circles are called **Concentric Circles**. They have no points of intersection but they have the same center and different radii.



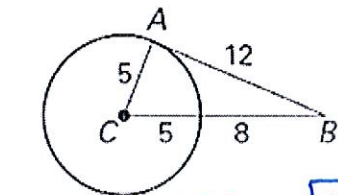
No Points of Intersection:

No points of intersection with different centers.

Tangent Theorems

Name	Theorem	Hypothesis	Conclusion
Perpendicular Tangent Theorem	If a line is tangent to a circle, then it is perpendicular to the radius drawn to the point of tangency.		If \overleftrightarrow{FD} is tangent to $\odot A$, then $\overline{AD} \perp \overleftrightarrow{FD}$
Converse of Perpendicular Tangent Theorem	If a line is perpendicular to a radius of a circle at a point on the circle, then the line is tangent to the circle.		If $\overline{AD} \perp \overleftrightarrow{FD}$, then \overleftrightarrow{FD} is tangent to $\odot A$
Tangent Segments Theorem	If two segments are tangent to a circle from the same external point, then the segments are congruent.		If \overline{CG} and \overline{BG} are tangent to $\odot A$ from point G, then $\overline{CG} \cong \overline{BG}$

Example: Is AB tangent to Circle C?



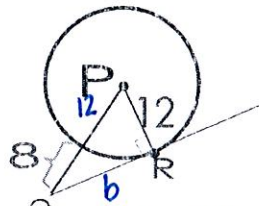
$$5^2 + 12^2 = 13^2$$

$$25 + 144 = 169$$

$$169 = 169 \checkmark$$

yes

Example: Find the length of RQ.



$RQ = 16$

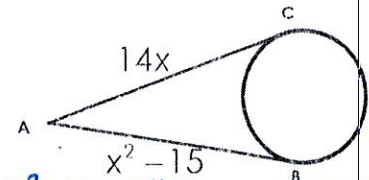
$$12^2 + b^2 = 20^2$$

$$144 + b^2 = 400$$

$$b^2 = 256$$

$$b = 16$$

Example: Find x.



$$x^2 - 15 = 14x$$

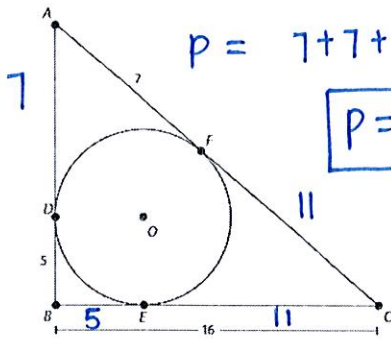
$$x^2 - 14x - 15 = 0$$

$$(x - 15)(x + 1) = 0$$

$$x = 15 \text{ and } x = -1$$

$x = 15$

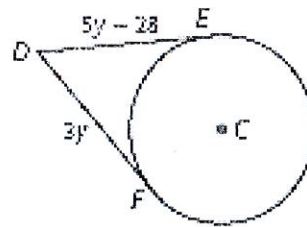
Example: Find perimeter of triangle ABC.



$$p = 7 + 7 + 11 + 11 + 5 + 5$$

$P = 46$

Example: Find DF if you know that DF and DE are tangent to $\odot C$.



$$5y - 28 = 3y$$

$$2y - 28 = 0$$

$$2y = 28$$

$$y = 14$$

$DF = 42$